

Binomial Theorem

IP Math

Pascal's Triangle		
n	$(a+b)^n$	Coefficients
0	$(a+b)^0 = 1$	
1	$(a+b)^1 = a+b$	
2	$(a+b)^2 = a^2 + 2ab + b^2$	1 2 1
3	$(a+b)^3 = a^3 + 3a^2b + 3ab^2 + b^3$	1 3 3 1
4	$(a+b)^4 = a^4 + 4a^3b + 6a^2b^2 + 4ab^3 + b^4$	14641
5	$(a+b)^{5} = a^{5} + 5a^{4}b + 10a^{3}b^{2} + 10a^{2}b^{3} + 5ab^{4} + b^{5}$	1 5 10 10 5 1

Topic Summary

Expansion of a binomial

$$(a+b)^{n} = a^{n} + {}^{n}C_{1}a^{n-1}b^{1} + {}^{n}C_{2}a^{n-2}b^{2} + \dots + {}^{n}C_{r}a^{n-r}b^{r} + \dots + b^{n}$$

General Term

In the expansion of $(a+b)^n$, the $(r+1)^{\text{th}}$ term is given as $\binom{n}{r}a^{n-r}b^r$

Binomial Theorem Practice Questions

- 1. Find the coefficient of x^2 in the expansion of $(1-3x)^2 \left(\frac{1}{\sqrt{x}} \sqrt[4]{x^3}\right)^8$.
- 2. (i) Expand $(1+x)^8$ in ascending powers of x, up to and including the term in x^3 .
 - (ii) In the expansion of $(1 + y + ky^2)^8$ in ascending powers of y, the coefficient of y^3 is zero. Find the value of the constant k.
- 3. Find the coefficient of x^5 in the expansion of $(1-2x+3x^2)^6$.
- 4. Write down and simplify the first three terms in the expansion, in ascending powers of x, of $\left(2-\frac{x}{4}\right)^{10}$. Hence find the coefficient of x^2 in the expansion of $\left(3+4x\right)^2 \left(2-\frac{x}{4}\right)^{10}$.

Answers

- 1. -420
- 2. (i) $(1+x)^8 = 1+8x+28x^2+56x^3+...$ (ii) k = -1
- 3. -2712
- 4. $1024 1280x + 720x^2$; -7856

